

*Polarization and Spin Effects in  
Neutralino Production and Decay  
MSSM and Extended Models*

*G. Moortgat-Pick  
University of Würzburg*

in collaboration with

*S. Hesselbach, F. Franke*

and

*A. Bartl, H. Fraas, W. Majerotto*

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Sitges

# Table of Contents

## *1. MSSM and Extended Models*

(NMSSM, E6 and SUSY LR-Model)

1.1 Neutralino Mass Spectra

1.2 Cross Sections

→ Influence of Beam Polarization

1.3 Decay Angular Distributions

→ Influence of Spin Correlations

→ Influence of Beam Polarization

## *2. MSSM without $M_1/M_2$ GUT Relation*

2.1  $M_1$  Dependence of  
Masses and Couplings

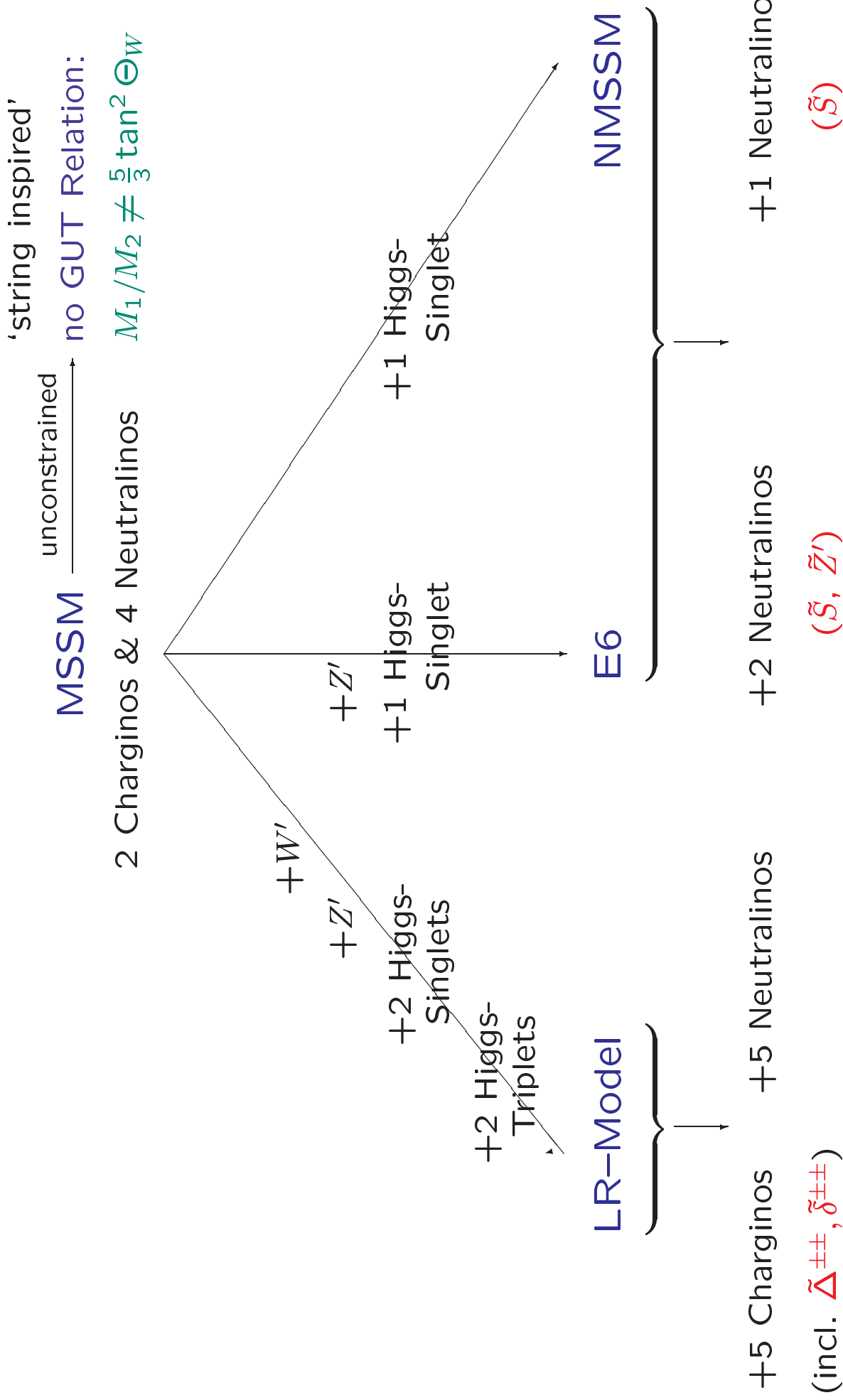
2.2  $M_1$  Dependence of:

- Cross Sections
- Polarization Asymmetries
- Forward–Backward Asymmetries

2.3 Influence of Slepton Masses

## *3. Conclusions*

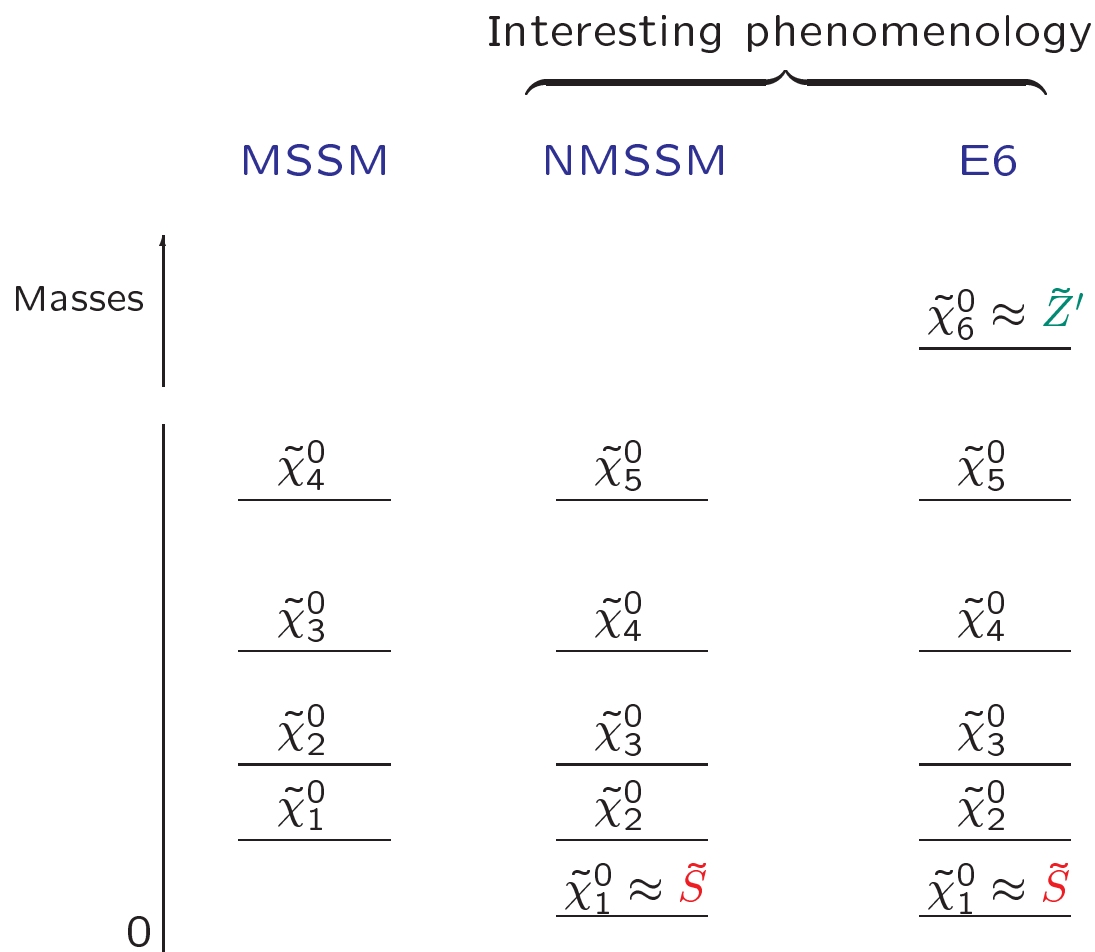
# 1. MSSM and Extended Models



## References

- **MSSM without  $M_1/M_2$  GUT Relation:**  
*Chen, Drees, Gunion ('95, '96); Feng et al. ('95, '97); Tsukamoto et al. ('95); Snowmass ('96); Kneur et al. ('98); Choi et al. ('98); M.-P. et al.('99);...*
- **NMSSM:**  
*Ellis et al. ('89); Kim, Oh, Stephan ('92, '93); Elliott, King, White ('93, '94); Franke ('94, '95, '96, '97); Ellwanger, Rausch de Trauenburg, Savoy ('93, '95, '97); Ellwanger, Hugonie ('97, '98, '99);...*
- **E6:**  
Model: *Hewett, Rizzo ('89); Boyce, Domcheski, König ('97);...*  
Neutralinos: *Gunion, Roszoski, Haber ('88); Cvetič et al. ('97); Gherghetta, Kaeding, Kane ('98); Nandi ('97); Keith, Ma ('96, '97); de Carlos, Espinosa ('97); Hesselbach, Franke, Fraas ('97); Suematsu ('97, '98); Hesselbach ('99);...*  
 $Z'$ -Physics: *Belanger, Godfrey ('86); Choudhury, Cuypers, Leike ('94); Godfrey ('95, '96); S. Riemann ('96); Hewett ('97); Leike, S. Riemann ('97); Rizzo ('97); Cho, Hagiwara, Matsumoto ('98);...*
- **SUSY-LR:**  
*Huitu, Maalampi, Raidal ('94); Aulakh, Melfo, Senjanovic ('96); Huitu et al. ('97); Raidal ('98); Raidal, Zerwas ('98); Huitu, Pandita, Puolamäki ('99);...*

# 1.1 Neutralino Mass Spectra



- Lightest neutralino (LSP)  $\tilde{\chi}_1^0 \approx$  Singlino  $\tilde{S}$

NMSSM: Franke '94  
 E6: de Carlos '97  
 Hesselbach '97

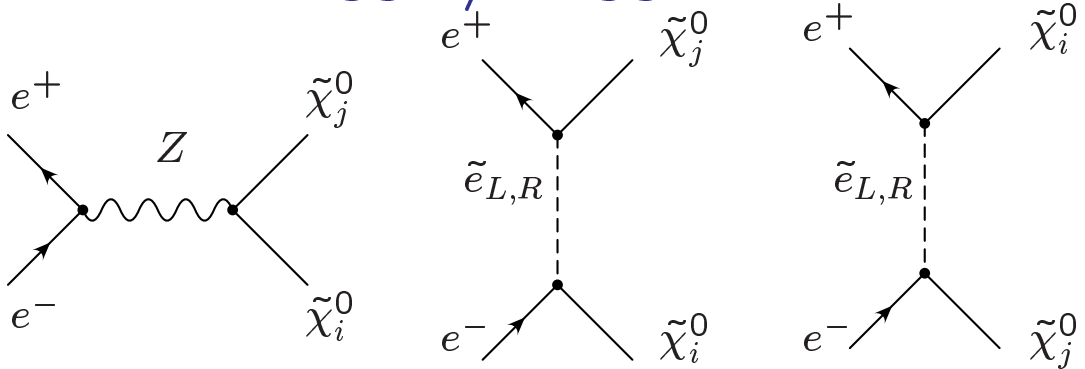
- $\tilde{S}$ : direct search is difficult  
 → produced in  $\tilde{\chi}_2^0$ -decay

# 1.2 Cross Sections

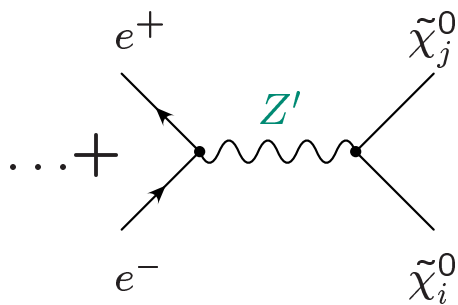
## Feynman Diagrams

$$e^+e^- \rightarrow \tilde{\chi}_i^0 \tilde{\chi}_j^0, \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 e^+ e^-$$

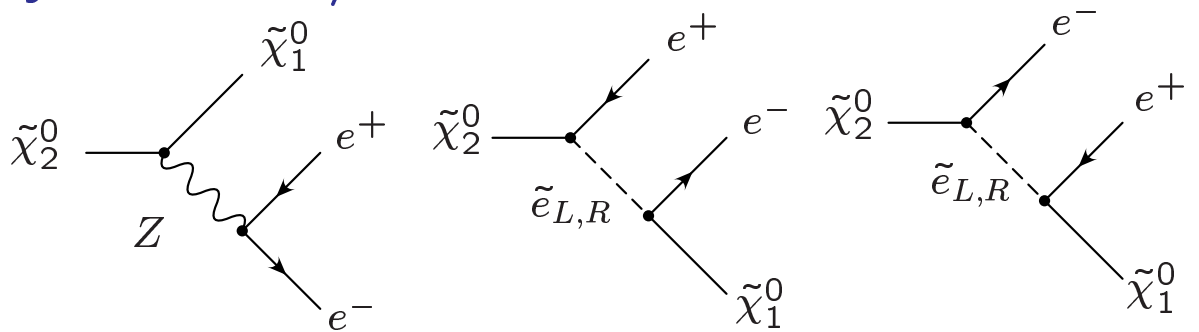
Production in MSSM/NMSSM:



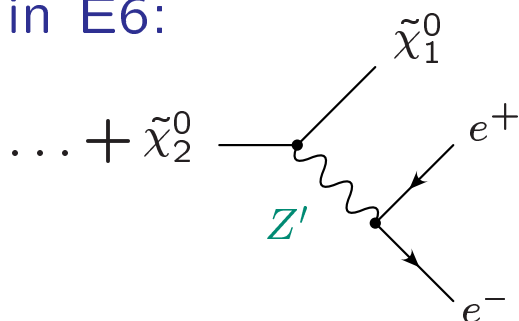
in E6:



Decay in MSSM/NMSSM:



in E6:



## Numerical Results

For this study:

- Gaugino-like light Neutralinos
- Neutralino masses:  $m_{\tilde{\chi}_1^0} = 72 \text{ GeV}$ ,  $m_{\tilde{\chi}_2^0} = 130 \text{ GeV}$   
→ same kinematics in all models
- Slepton masses:  $m_{\tilde{e}_L} = 197 \text{ GeV}$ ,  $m_{\tilde{e}_R} = 160 \text{ GeV}$
- NMSSM, E6:  $\tilde{\chi}_1^0 \approx \tilde{S}$  (=LSP)
- Polarization of **both** beams:  
 $P_{e^-} = \pm 85\%$ ,  $P_{e^+} = \pm 60\%$   
Notation:  $(\text{sgn}(P_{e^-})\text{sgn}(P_{e^+}))$ , left-handed:  $-$   
right-handed:  $+$
- High Luminosity  $\mathcal{L}^h = 500 \text{ fb}^{-1}$   
Low Luminosity  $\mathcal{L}^l = 50 \text{ fb}^{-1}$

Comparison of MSSM, NMSSM, E6:

- Production Cross Section  $\sigma(\sqrt{s})$
- Decay Angular Distribution and Forward–Backward–Asymmetry  $A_{FB}$  in the lab–system

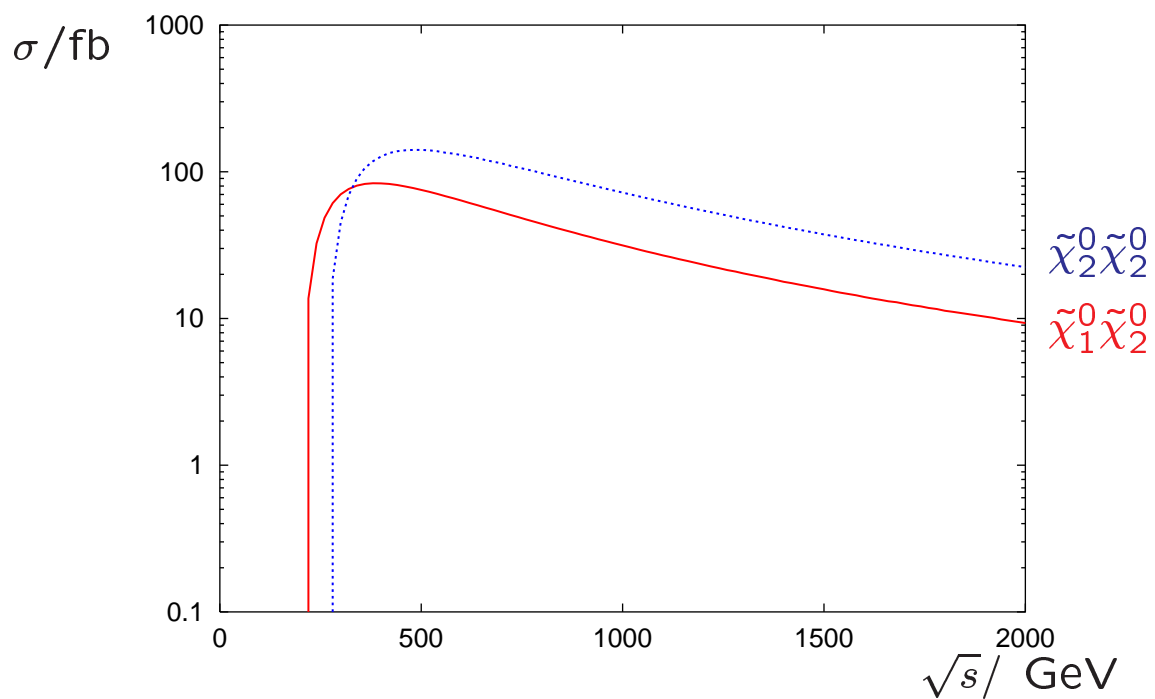
## 1.2.1 Neutralino Production in MSSM

gaugino-like:  
([mass]=GeV)

$M_2$	$\mu$	$\tan \beta$
152	316	3

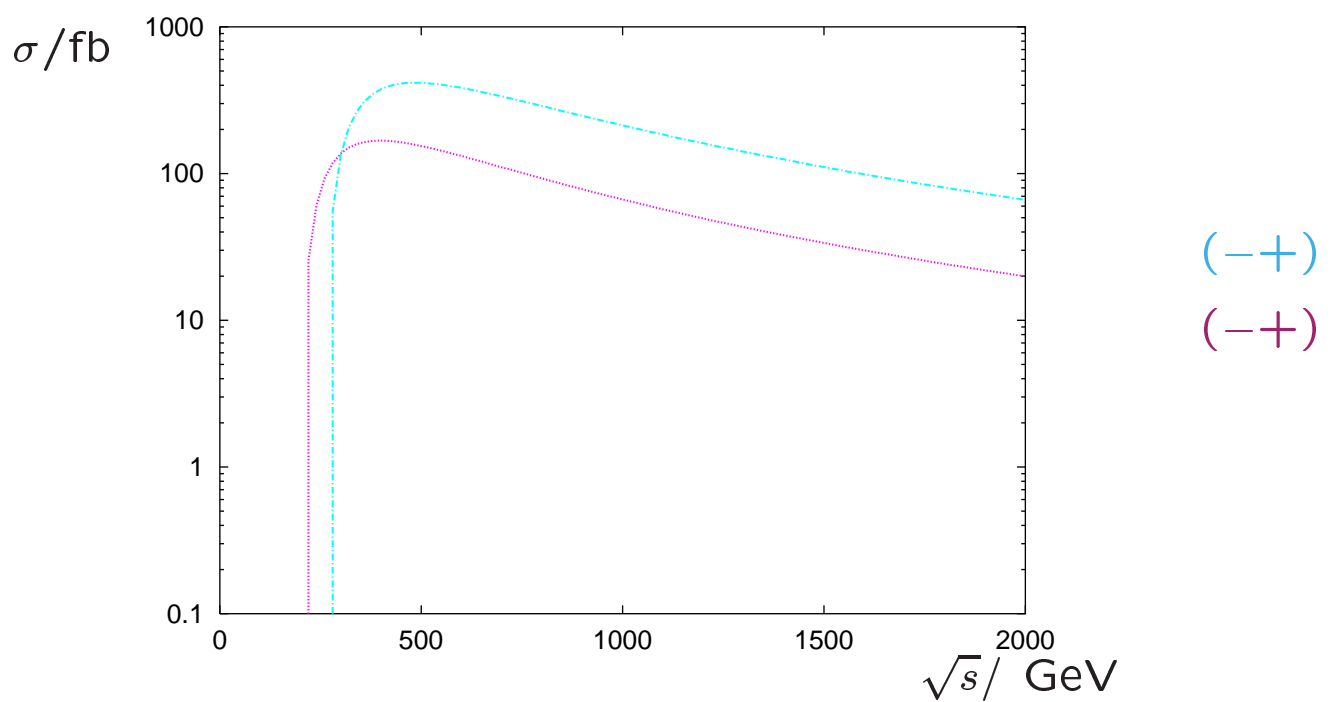
(Ambrosanio,  
Blair, Zerwas '98)

$$\sigma = \sigma(e^+e^- \rightarrow \tilde{\chi}_i^0 \tilde{\chi}_j^0) \text{ for } (00)$$





and  $(-+)$ :



- highest  $\sigma$  for  $(-+)$
- $\sigma(-+)/\sigma(00) \sim 2 - 3$

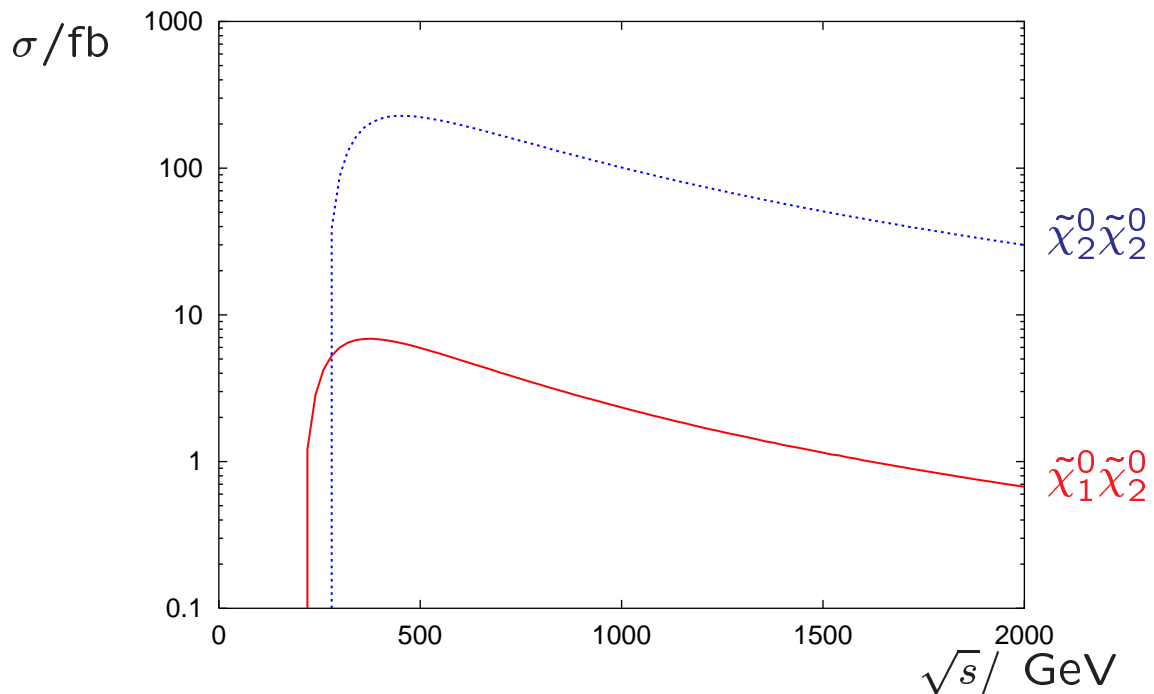
## 1.2.2 Neutralino Production in NMSSM

NMSSM parameters ( $\lambda v_3 \hat{=} \mu$ ):

$M_2$	$\tan \beta$	$\lambda$	$v_3$	$\kappa$
262	3	0.9	1000	0.0295

([mass]=GeV)

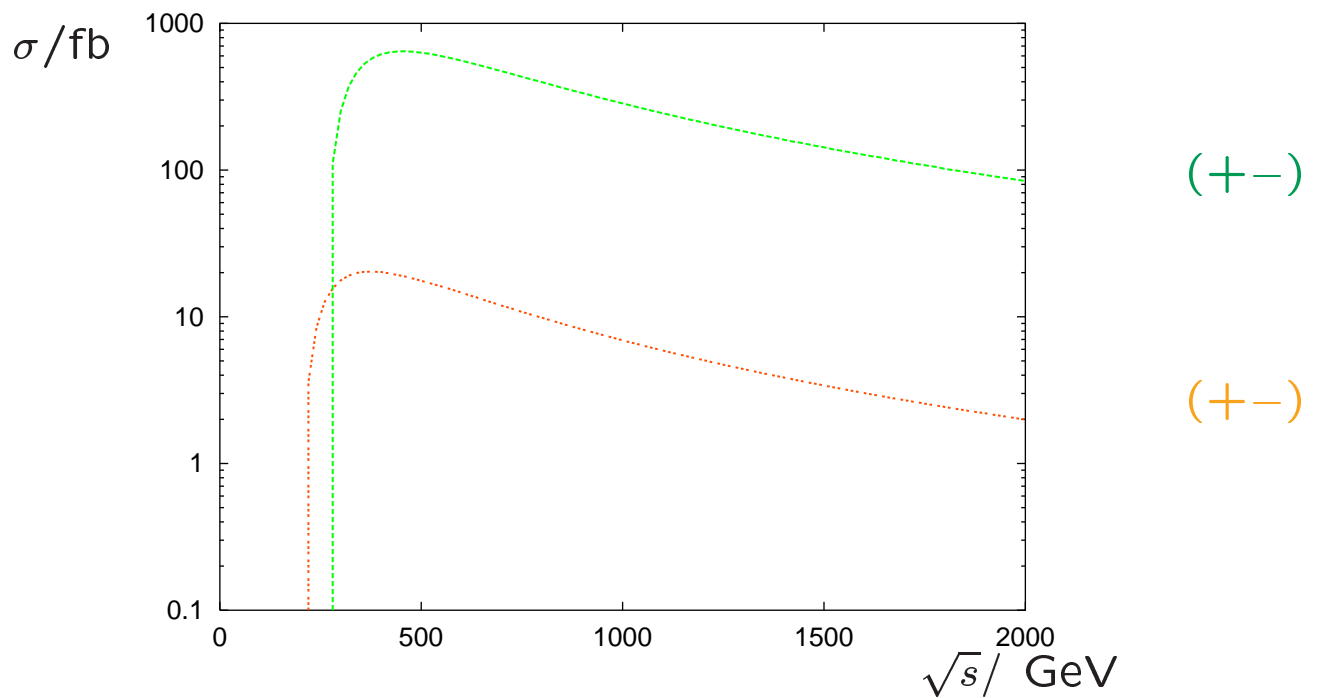
$$\sigma = \sigma(e^+e^- \rightarrow \tilde{\chi}_i^0 \tilde{\chi}_j^0) \text{ for } (00)$$



- $\tilde{\chi}_1^0 \approx \tilde{S}$  couples very weakly  $\rightarrow$  small  $\sigma$
- if ,  $\tilde{\chi}_2^0 < 10^{-12}$  GeV  $\Rightarrow$  **displaced vertices**
- if ,  $\tilde{\chi}_2^0 < 10^{-16}$  GeV  $\Rightarrow$  escapes detection

Hugonie et al. '98

and  $(+-)$ :



- highest  $\sigma$  for  $(+-)$  → contrary to MSSM!
- $\sigma(+ -)/\sigma(00) \sim 3$

## 1.2.3 Neutralino Production in E6

E6 parameters ( $\lambda v_3 = \mu$ ):

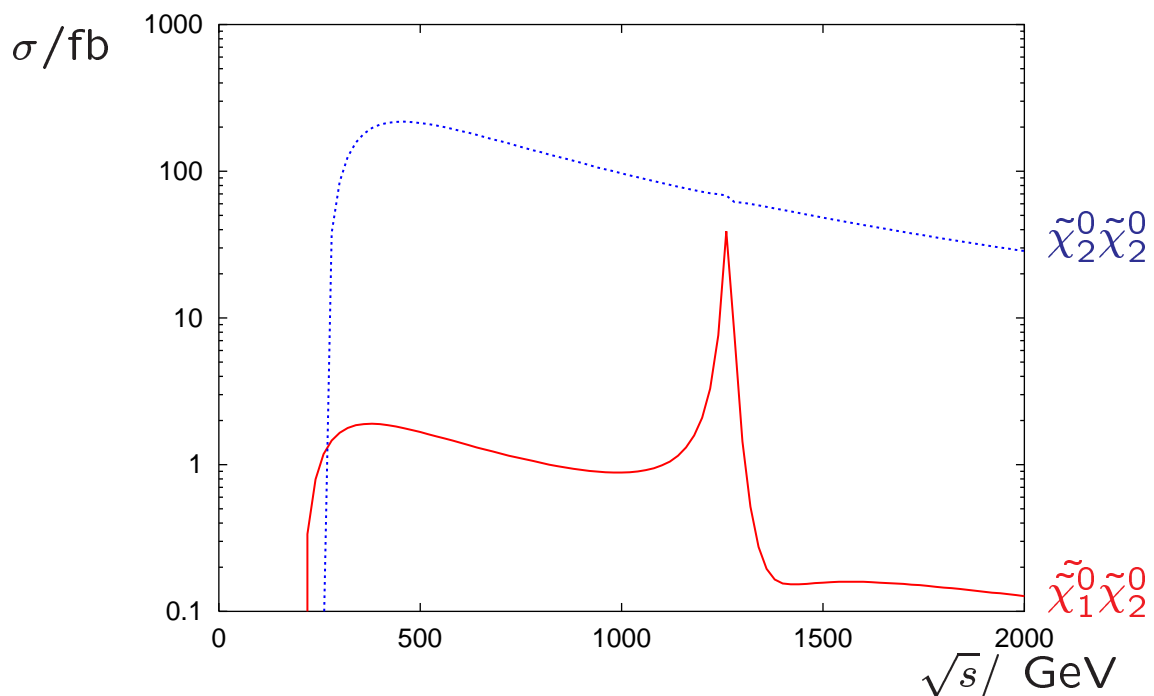
$M_2$	$\tan \beta$	$M'$	$\lambda$	$v_3$	
270	3	22300	0.15	3000	([mass]=GeV)

$$m_{Z'} = 1264 \text{ GeV}$$

$$\Gamma_{Z'} = 0.014 m_{Z'}$$

Gherghetta et al.'98

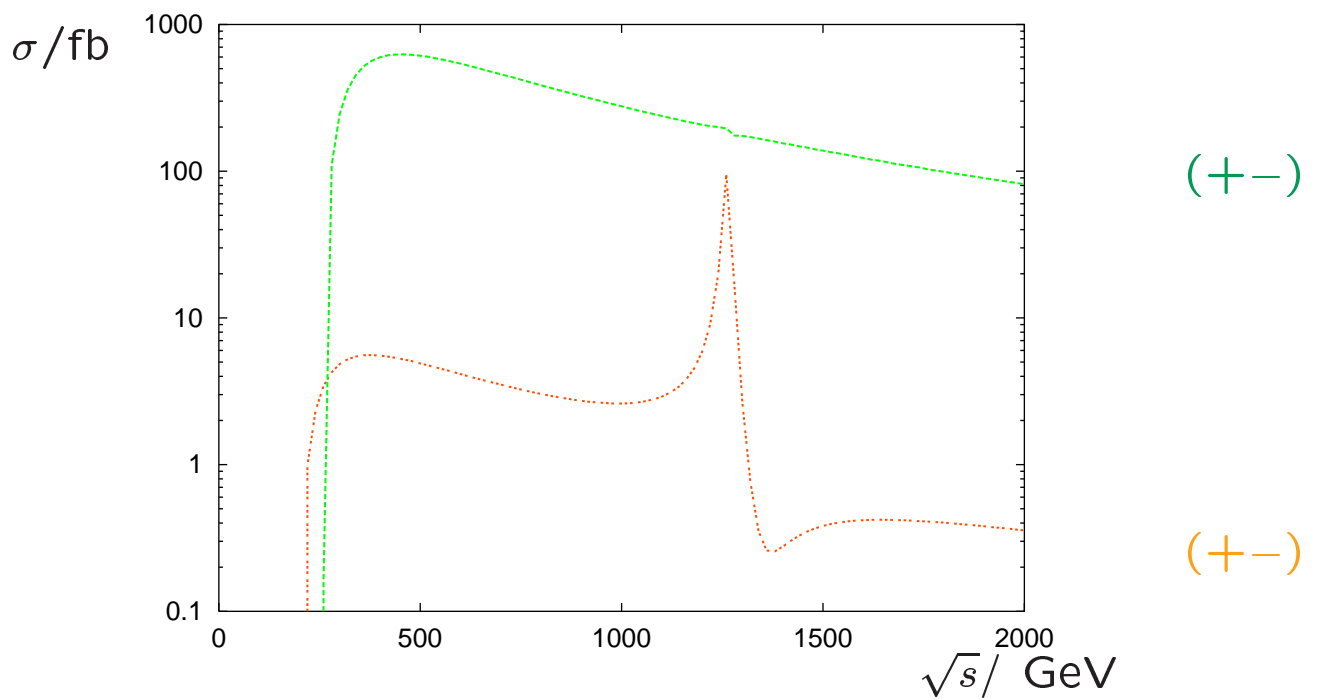
$$\sigma = \sigma(e^+ e^- \rightarrow \tilde{\chi}_i^0 \tilde{\chi}_j^0) \text{ for } (00)$$



- $\tilde{\chi}_1^0 \approx \tilde{S}$  couples to  $Z'$   $\rightarrow$  peak at  $\approx \sqrt{s} = 1264$  GeV
- $\tilde{\chi}_2^0$  (gaugino-like): very small coupling to  $Z'$   
 $\rightarrow$  almost no  $Z'$  peak
- **displaced vertices** also possible

Hesselbach '99

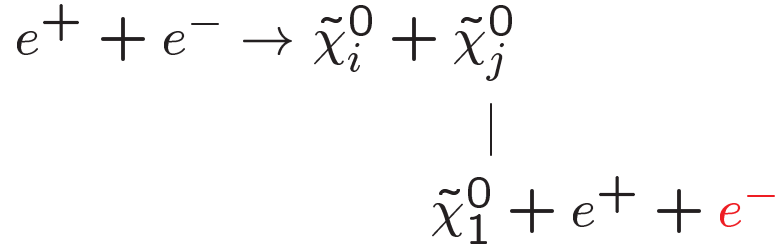
and (+-):



- highest  $\sigma$  for (+-): **contrary** to MSSM!
- $\sigma(+\text{-})/\sigma(00) \sim 3$

## 1.3 Decay Angular Distribution of $e^-$ in the Laboratory System

*Neutralino production and leptonic decay:*



⇒ Including complete **spin correlations** between production and decay!

M.-P. et al. '97, '99

*Amplitude squared of production × decay:*

$$|T|^2 \sim \mathcal{P}(p_j, \underbrace{s_j, p_i, s_i}_{\text{spin correlations}}) \otimes \underbrace{\mathcal{D}(p_i, s_i)}_{\text{spin correlations}} \otimes \mathcal{D}(p_j, s_j)$$

$$\sim \left( \begin{array}{l} P_{ij} \cdot D_i \cdot D_j \\ + S_j^P(s_j) \otimes S_j^D(s_j) \cdot D_i \\ + S_i^P(s_i) \otimes S_i^D(s_i) \cdot D_j \\ + S_{ij}^P(s_i, s_j) \otimes S_i^D(s_i) \otimes S_j^D(s_j) \end{array} \right) \begin{array}{l} \rightarrow \text{no correlations} \\ \\ \\ \end{array} \Bigg\} = 0 \text{ if } \tilde{\chi}_i^0 = \tilde{\chi}_1^0$$

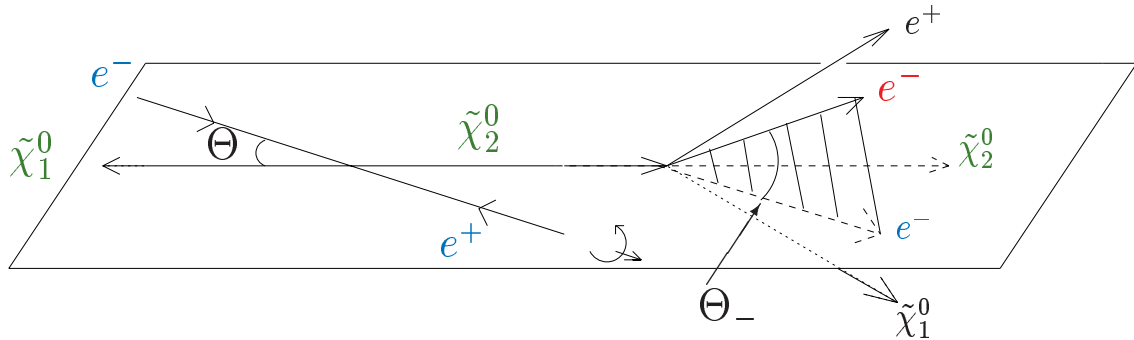
$$\mathcal{P}(p_i, s_i, p_j, s_j) = P_{ij} + S_i^P(s_i) + S_j^P(s_j) + S_{ij}^P(s_i, s_j)$$

$$\mathcal{D}(p_i, s_i) = D_i + S_i^D(s_i)$$

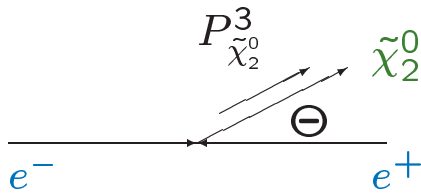
$$\mathcal{D}(p_j, s_j) = D_j + S_j^D(s_j) \qquad (s_i(s_j) : \text{spin vector of } \tilde{\chi}_i^0(\tilde{\chi}_j^0))$$

# Decay Angular Distribution of $e^-$ in the Laboratory System

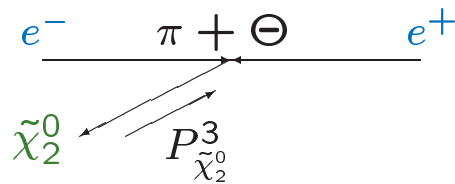
$$e^+e^- \rightarrow \tilde{\chi}_1^0\tilde{\chi}_2^0, \quad \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0e^+e^-$$



- Production:  
No forward-backward asymmetry!  
(Majorana fermions!)
- Production  $\times$  Decay:  
Decay angular distribution of  $e^-$  depends on polarization of  $\tilde{\chi}_2^0$ , e.g.  $P_{\tilde{\chi}_2^0}^3 \sim \cos \Theta$



$$P_{\tilde{\chi}_2^0}^3 > 0$$



$$P_{\tilde{\chi}_2^0}^3 < 0$$

$\Rightarrow$  Spin correlations between production and decay

$\Rightarrow$  Large forward-backward-asymmetry of

decay  $e^-$  possible:  $A_{FB} = \frac{\sigma(\cos \Theta_- > 0) - \sigma(\cos \Theta_- < 0)}{\sigma(\cos \Theta_- > 0) + \sigma(\cos \Theta_- < 0)}$

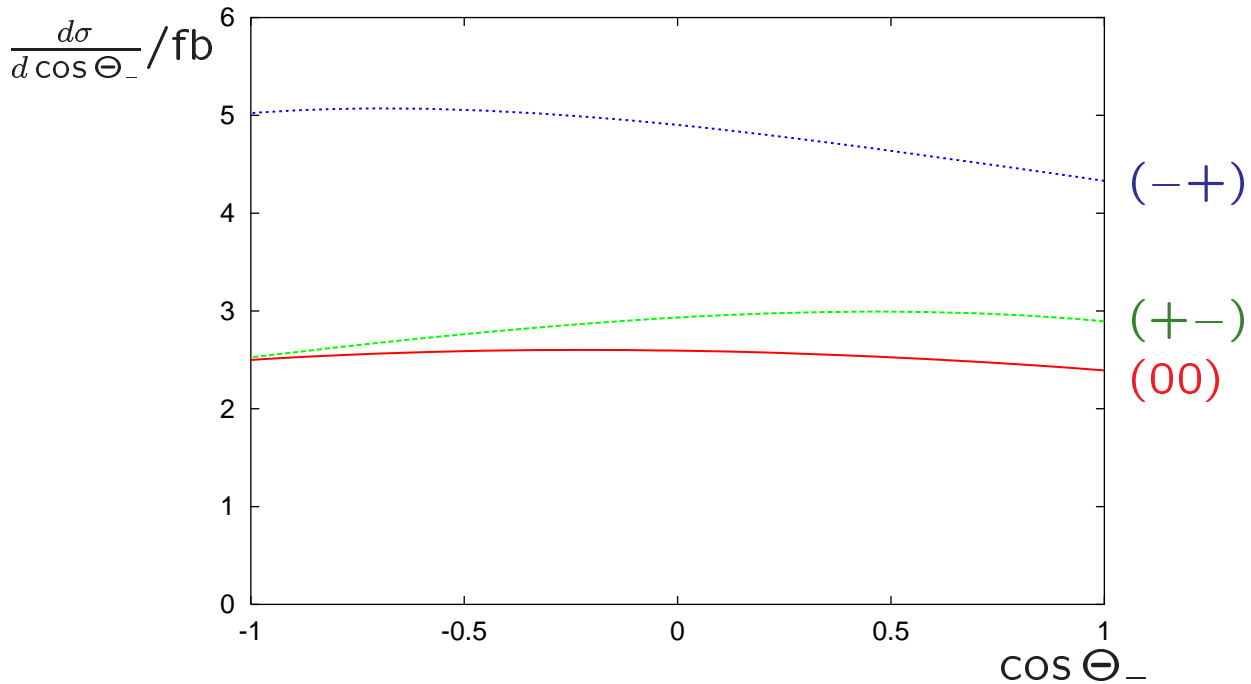
- Cross Section:  $\sigma_e = \sigma \times BR = \int \frac{d\sigma}{d \cos \Theta_-} d \cos \Theta_-$

## 1.3.1 Decay Angular Distribution in MSSM

gaugino-like:  
([mass]=GeV)

$M_2$	$\mu$	$\tan \beta$
152	316	3

$$\sqrt{s} = m_{\tilde{\chi}_1^0} + m_{\tilde{\chi}_2^0} + 50 \text{ GeV}$$



	$A_{FB}(\mathcal{L}^h) / \%$	$A_{FB}(\mathcal{L}^l) / \%$	$\sigma_e(\mathcal{L}^h) / \text{fb}$	$\sigma_e(\mathcal{L}^l) / \text{fb}$
(00)	$-1.2 \pm 1.9$	$-1.2 \pm 6.3$	$5.1 \pm 0.1$	$5.1 \pm 0.3$
(-+)	$-4.1 \pm 1.4$	$-4.1 \pm 4.5$	$9.7 \pm 0.1$	$9.7 \pm 0.4$
(+-)	$+3.8 \pm 1.8$	$+3.8 \pm 5.9$	$5.7 \pm 0.1$	$5.7 \pm 0.3$

- **Strong** influence of spin correlations  
→ result without spin correlations:  $A_{FB} = 0.1\%$
- Beam polarization **changes** angular distribution!
- other gaugino scenarios: larger  $A_{FB}$  up to 15%

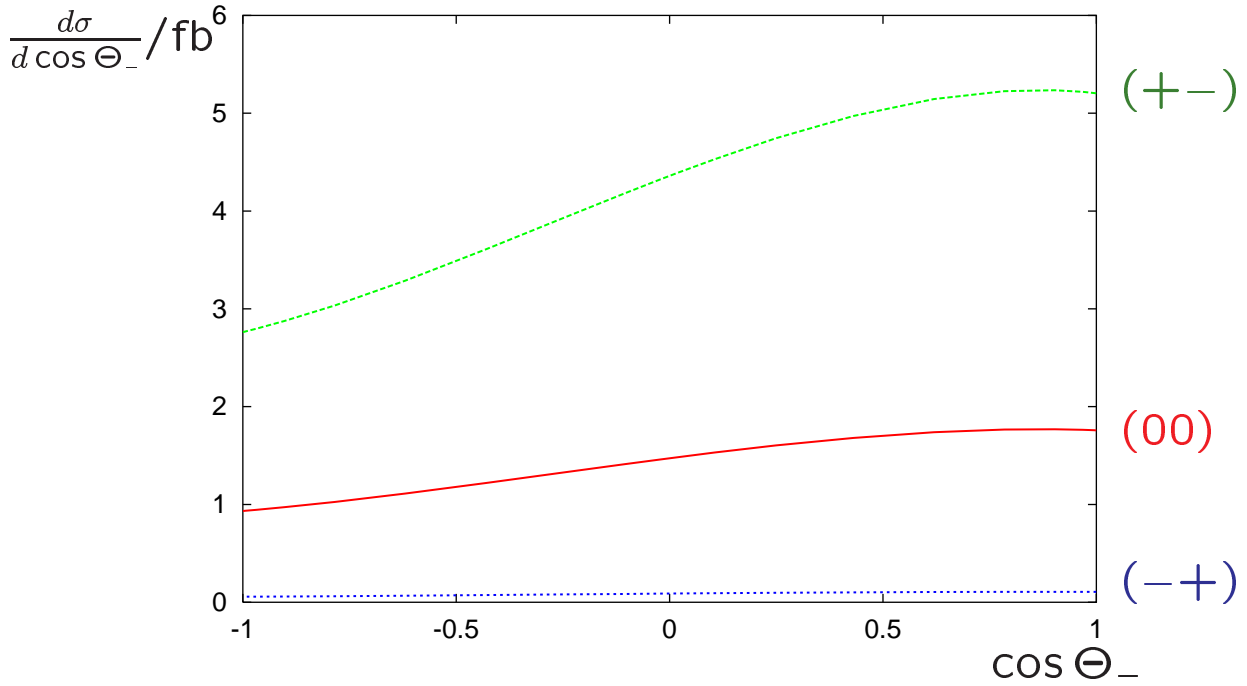
M.-P. '97,'98



## 1.3.2 Decay Angular Distribution in NMSSM

$M_2$	$\tan \beta$	$\lambda$	$v_3$	$\kappa$	([mass]=GeV)
262	3	0.9	1000	0.0295	

$$\sqrt{s} = m_{\tilde{\chi}_1^0} + m_{\tilde{\chi}_2^0} + 50 \text{ GeV}$$



	$A_{FB}(\mathcal{L}^h) / \%$	$A_{FB}(\mathcal{L}^l) / \%$	$\sigma_e(\mathcal{L}^h) / \text{fb}$	$\sigma_e(\mathcal{L}^l) / \text{fb}$
(00)	$+17.1 \pm 2.6$	$+17.1 \pm 8.2$	$2.9 \pm < 0.1$	$2.9 \pm 0.2$
(-+)	$+16.9 \pm 10.7$	$+16.9 \pm 33.8$	$0.17 \pm < 0.1$	$0.17 \pm 0.1$
(+-)	$+17.1 \pm 1.5$	$+17.1 \pm 4.8$	$8.5 \pm 0.1$	$8.5 \pm 0.4$

- **Strong** influence of spin correlations  
 $\Rightarrow$  large  $A_{FB}$
- Small  $\sigma_e \Rightarrow \mathcal{L}^h$  essential

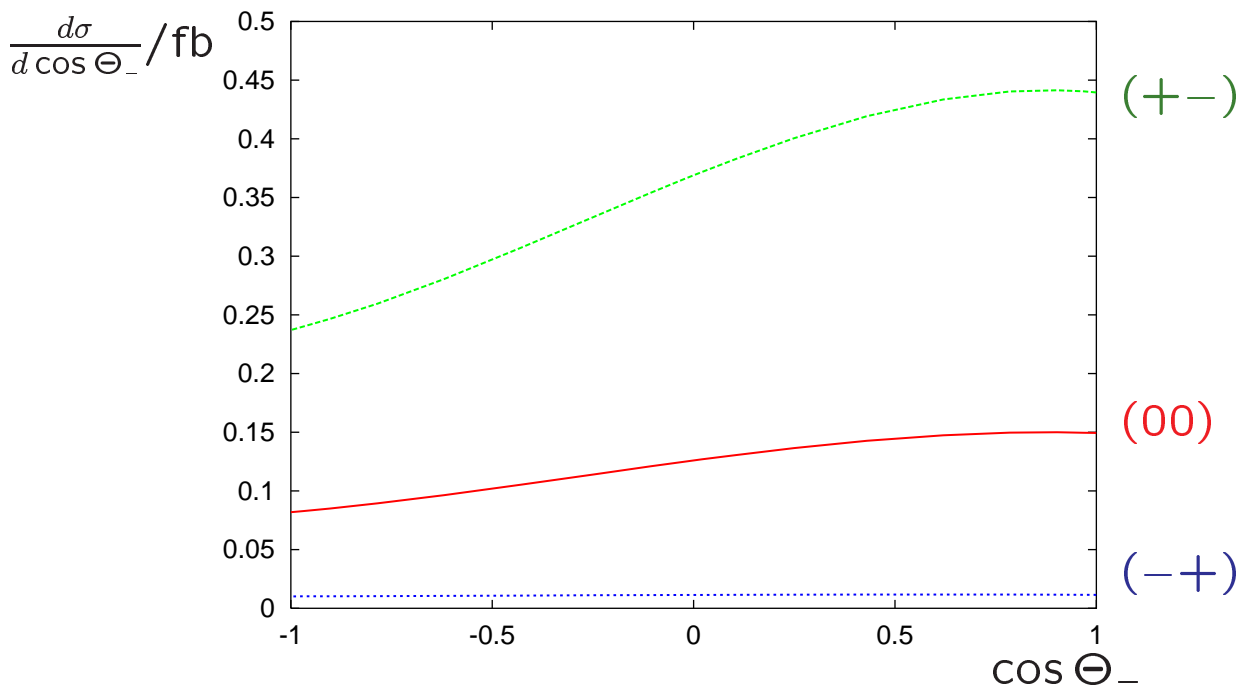
### 1.3.3 Decay Angular Distribution in E6

gaugino-like:

$M_2$	$\lambda$	$v_3$	$M'$	$\tan \beta$
-270	0.15	3000	22300	3

([mass]=GeV)

$$\sqrt{s} = m_{\tilde{\chi}_1^0} + m_{\tilde{\chi}_2^0} + 50 \text{ GeV}$$

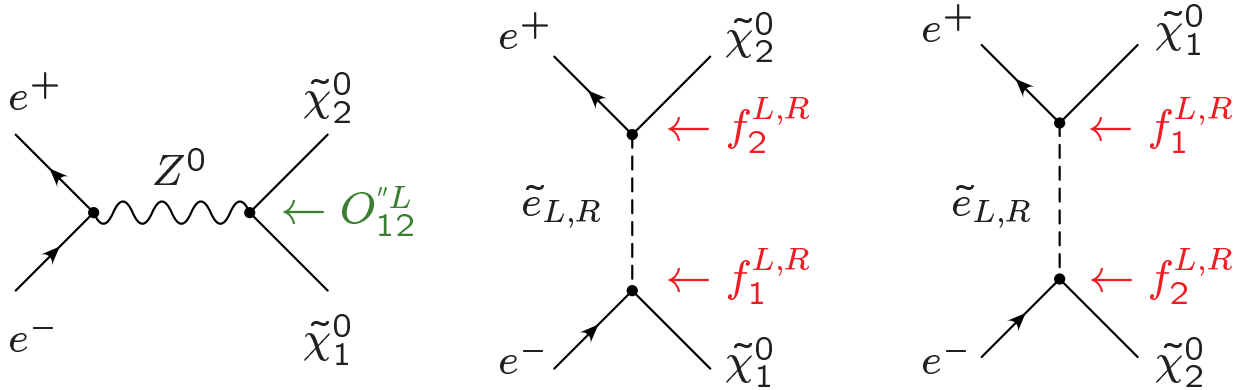


	$A_{FB}(\mathcal{L}^h) / \%$	$A_{FB}(\mathcal{L}^l) / \%$	$\sigma_e(\mathcal{L}^h) / \text{fb}$	$\sigma_e(\mathcal{L}^l) / \text{fb}$
(00)	$+16.2 \pm 8.8$	$+16.2 \pm 27.9$	$0.25 \pm 0.02$	$0.25 \pm 0.07$
(-+)	$+3.9$	$+3.9$	$0.02$	$0.02$
(+-)	$+16.6 \pm 5.2$	$+16.6 \pm 16.4$	$0.72 \pm 0.04$	$0.72 \pm 0.12$

- Here: angular dependence similar to NMSSM
- very small  $\sigma_e \Rightarrow$  highest  $\mathcal{L}^h$  necessary
- Polarization of *both* beams useful

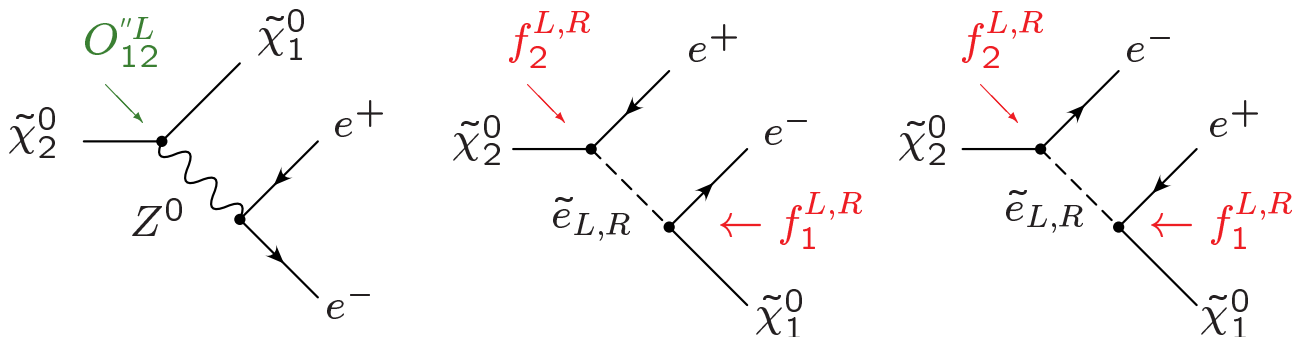
## 2. MSSM without $M_1/M_2$ GUT-Relation Feynman Diagrams

### Production:



$Z^0$  and left and right selectron exchange

### Decay:



$Z^0$  and left and right selectron exchange

$$M_1 \Rightarrow \begin{cases} \text{couplings: } f_1^L f_2^L, f_1^R f_2^R, O''_{12}{}^L \\ \text{neutralino masses: } m_{\tilde{\chi}_1^0}, m_{\tilde{\chi}_2^0} \end{cases}$$

## 2.1 $M_1$ Dependence on Masses and Couplings

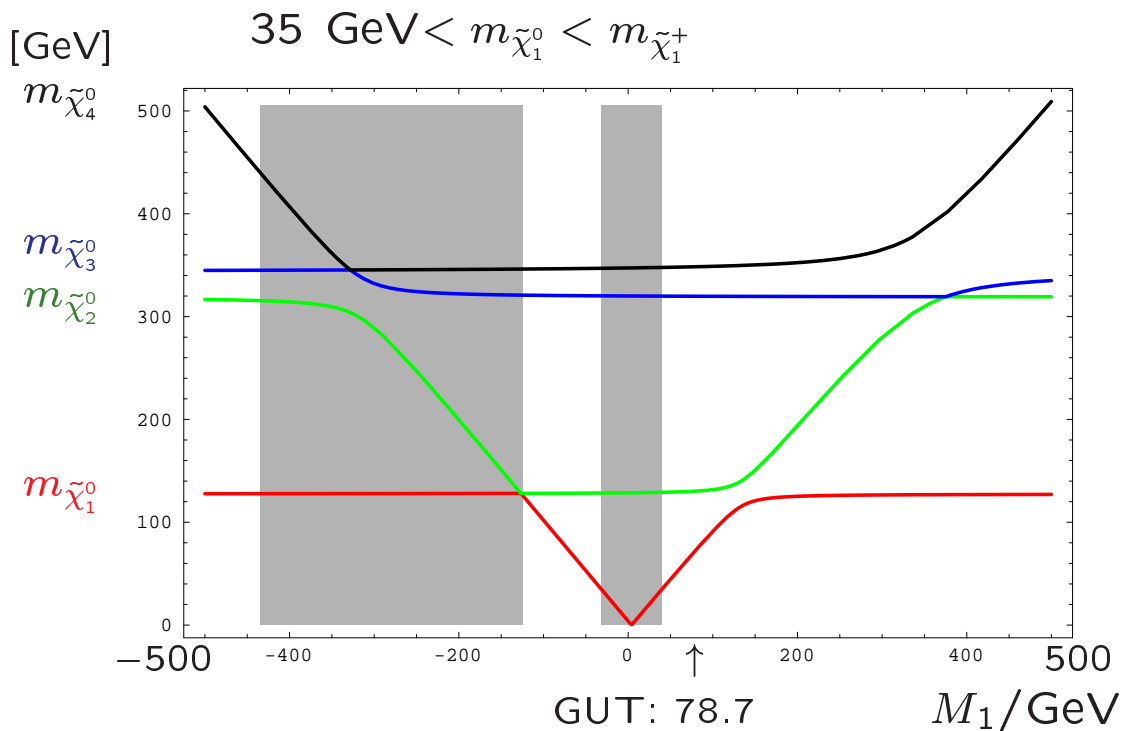
### 2.1.1 Neutralino Masses

gaugino-like:

([mass]=GeV)

$M_2$	$\mu$	$\tan \beta$	$m_{\tilde{\chi}_1^\pm}$
152	316	3	128

Neutralino mass spectrum:



→  $|M_1| < 150 \text{ GeV}$ : strong influence on  $m_{\tilde{\chi}_1^0}$

→  $150 < M_1 < 380 \text{ GeV}$ : strong influence on  $m_{\tilde{\chi}_2^0}$

$m_{\tilde{\chi}_2^0} > m_{\tilde{e}_{L,R}}$ : two-body decays

→ **degeneracy** possible:  $m_{\tilde{\chi}_1^0} \approx m_{\tilde{\chi}_1^\pm}$ ,  $m_{\tilde{\chi}_1^0} \approx m_{\tilde{\chi}_2^0}$ ,

⇒ soft decay lepton spectrum

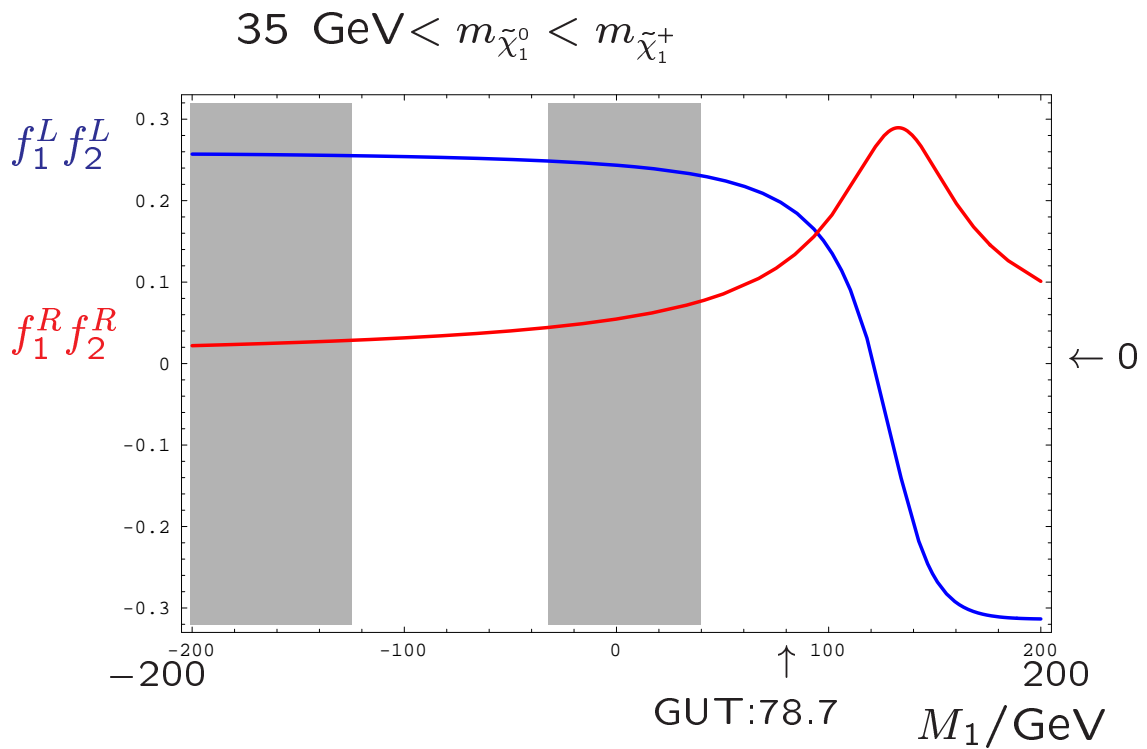
Drees et al. '95, '96

## 2.1.2 $M_1$ Dependence of $\tilde{\chi}_i^0 \tilde{e}e$ -couplings

gaugino-like:

$M_2$	$\mu$	$\tan \beta$	$m_{\tilde{\chi}_1^\pm}$
152	316	3	128

([mass]=GeV)



- $f_1^R f_2^R > 0$ : maximum at  $M_1 \approx 140$  GeV
- $f_1^L f_2^L$ : changes sign at  $M_1 \approx 120$  GeV!

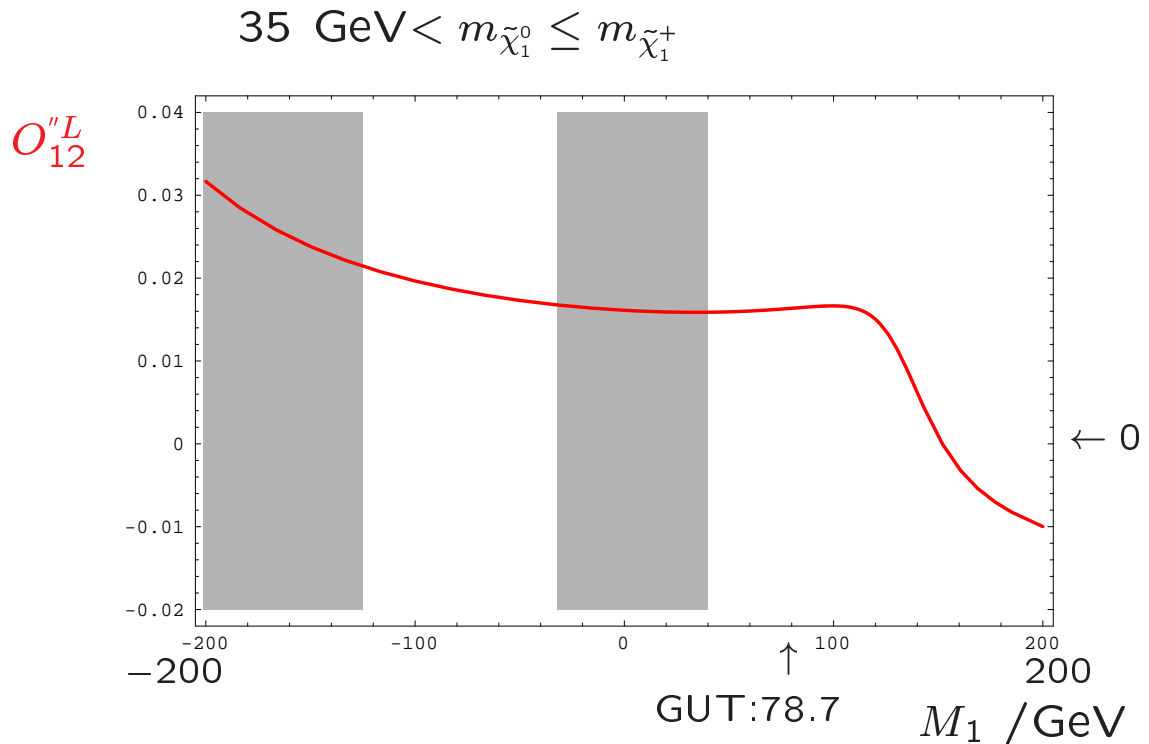
⇒ Studied range for  $M_1 = [40, 160]$  GeV

## 2.1.3 $M_1$ Dependence of $\tilde{\chi}_i^0 \tilde{\chi}_j^0 e$ -couplings

gaugino-like:

$M_2$	$\mu$	$\tan \beta$	$m_{\tilde{\chi}_1^\pm}$
152	316	3	128

([mass]=GeV)



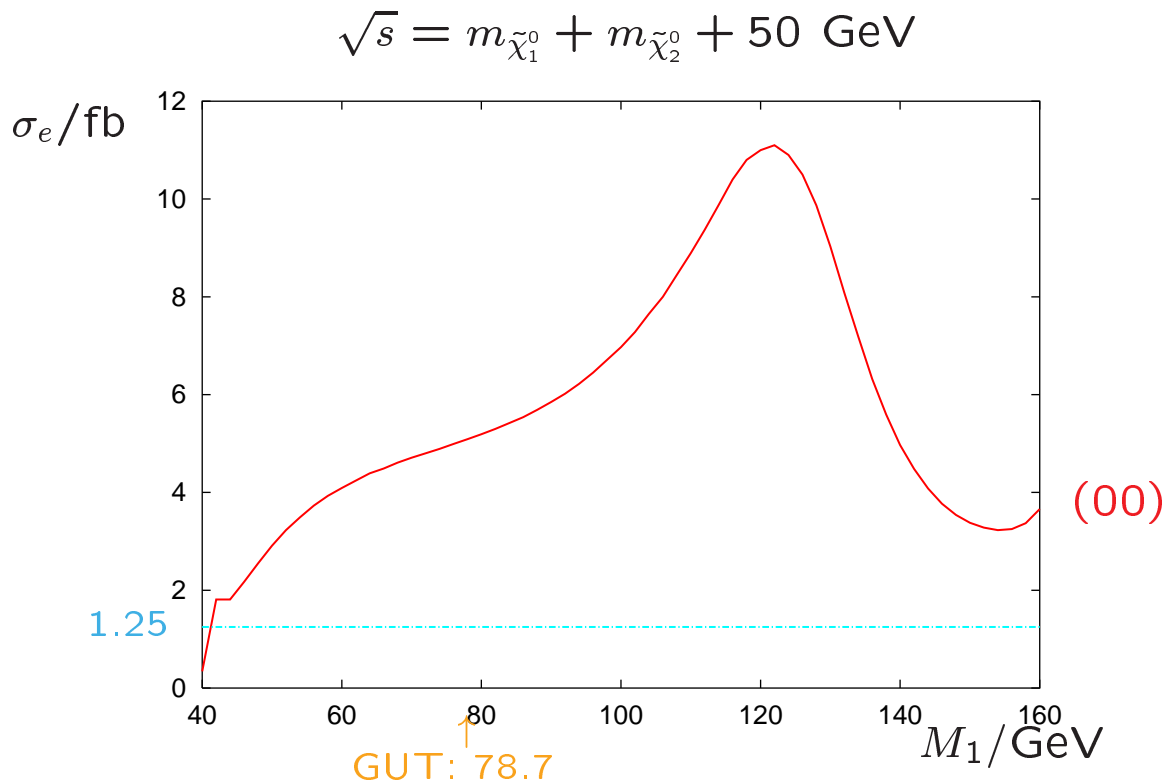
- $M_1 < 115 \text{ GeV}$ :  $O''_{12}^L \approx \text{const.}$  and small
- $M_1 > 115 \text{ GeV}$ :  $O''_{12}^L$  decreases

$\Rightarrow M_1 = [40, 160] \text{ GeV}$ : small influence of  $Z^0$ -exchange

## 2.2.1 $M_1$ Dependence of $\sigma_e$

$M_2$	$\mu$	$\tan \beta$	$m_{\tilde{e}_L}$	$m_{\tilde{e}_R}$	[mass]=GeV
152	316	3	197	160	

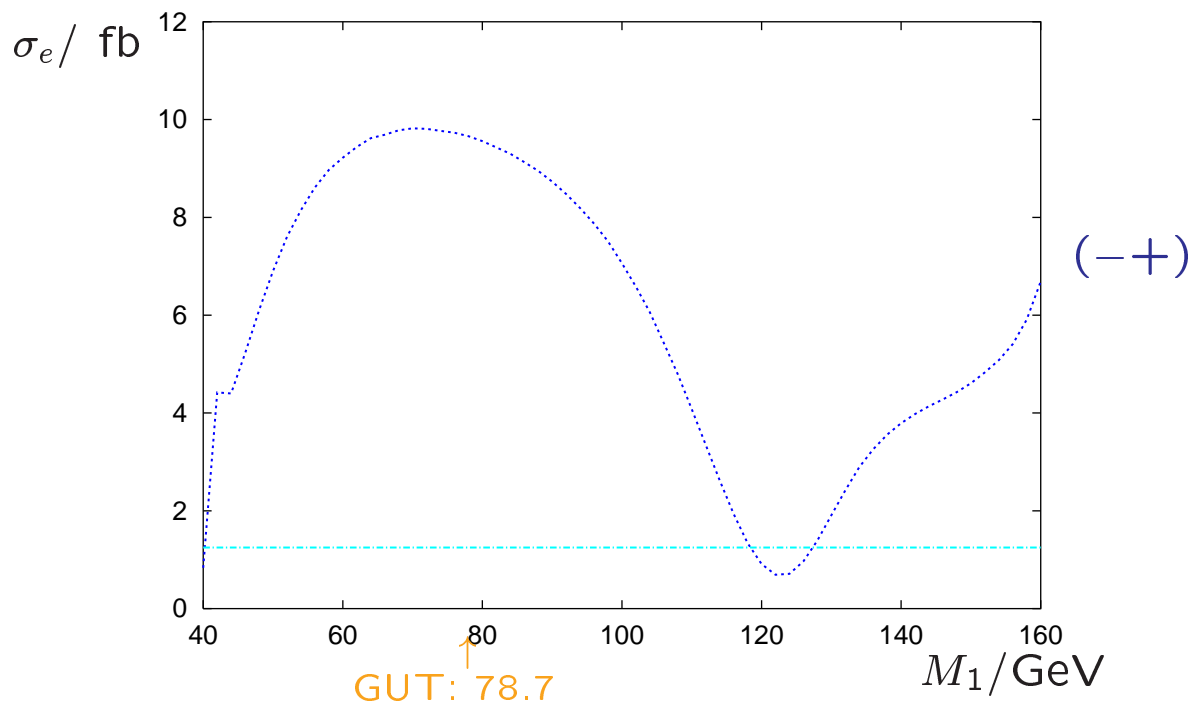
Cross sections for (00)



- **strong**  $M_1$  dependence  
→ influence of slepton couplings
- for Asymmetries  $\geq 4\%$  (up to '1  $\sigma$ '):  
for  $\mathcal{L}^h$ :  $\sigma_e \geq 1.25 \text{ fb}$   
for  $\mathcal{L}^l$ :  $\sigma_e \geq 12.5 \text{ fb}$  (not reached!)

and  $(-+)$ :

$$\sqrt{s} = m_{\tilde{\chi}_1^0} + m_{\tilde{\chi}_2^0} + 50 \text{ GeV}$$



- $M_1$  dependence of  $\sigma_e$  changes strongly  
→ influence of **beam polarization**

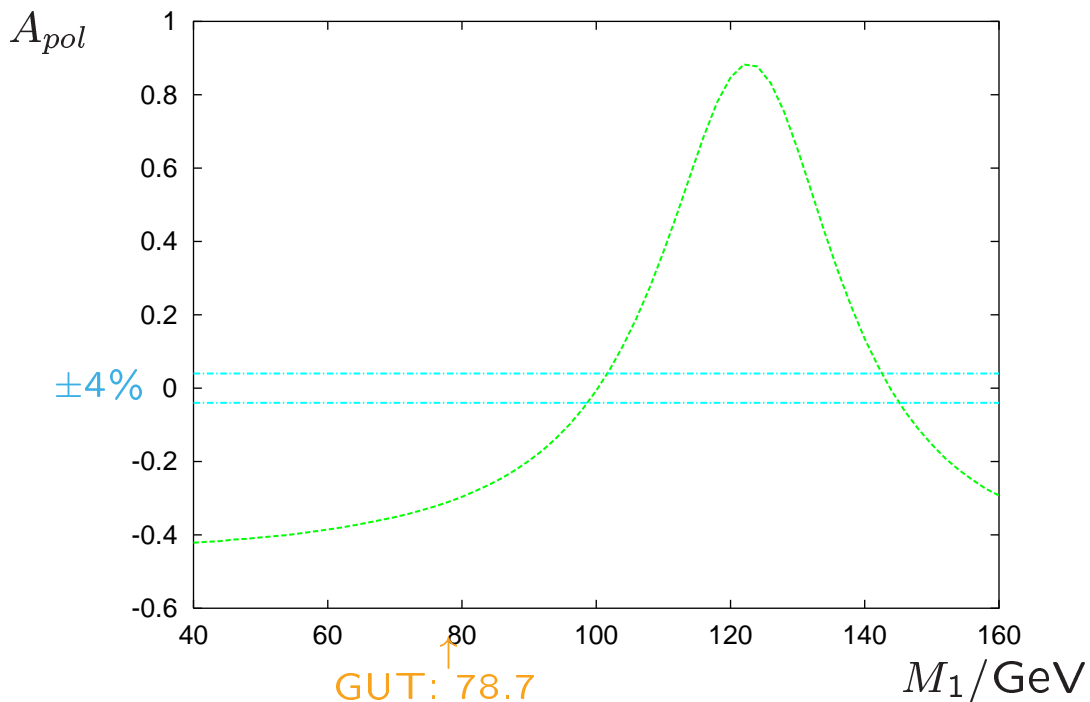


## 2.2.2 $M_1$ Dependence of Polarization Asymmetry

$M_2$	$\mu$	$\tan \beta$	$m_{\tilde{e}_L}$	$m_{\tilde{e}_R}$	[mass]=GeV
152	316	3	197	160	

$$A_{pol} := [\sigma_e(00) - \sigma_e(-+)] / [\sigma_e(00) + \sigma_e(-+)]$$

$$\sqrt{s} = m_{\tilde{\chi}_1^0} + m_{\tilde{\chi}_2^0} + 50 \text{ GeV}$$



- strong  $M_1$  dependence
- for  $\mathcal{L}^h$ :  $A_{pol} \geq 4\%$  in almost the whole region
- for high slepton mass splitting  
 $\Rightarrow$  weak  $M_1$  dependence

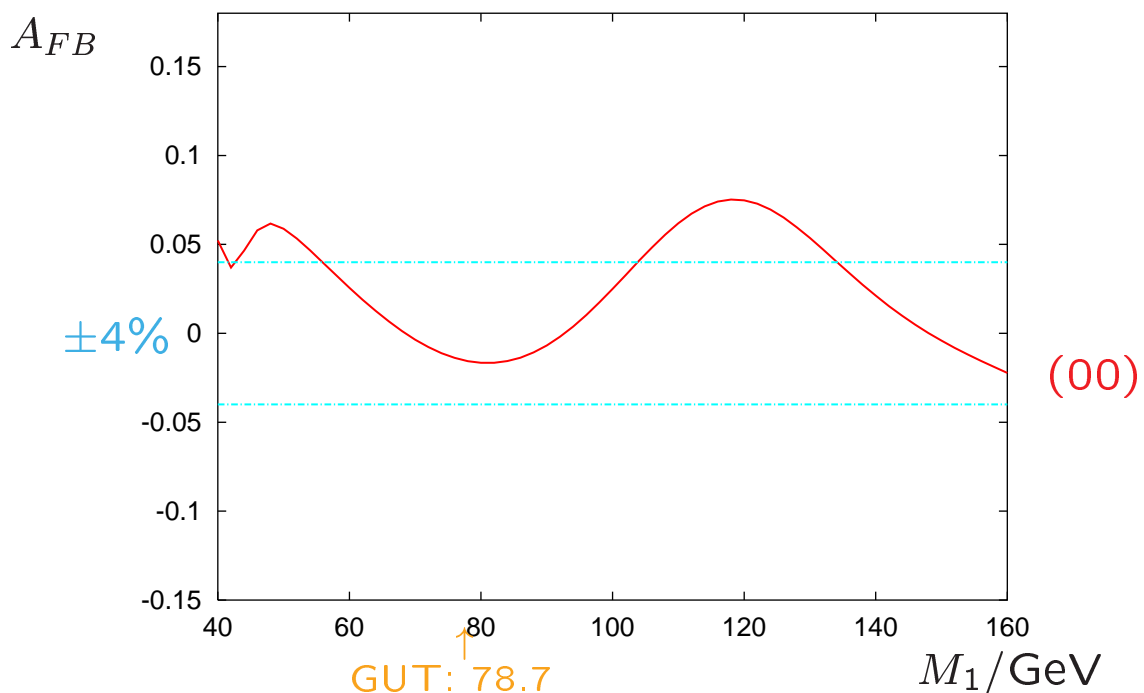
M.-P. '99

## 2.2.3 $M_1$ Dependence of $A_{FB}$ in Lab-system

$M_2$	$\mu$	$\tan \beta$	$m_{\tilde{e}_L}$	$m_{\tilde{e}_R}$	[mass]=GeV
152	316	3	197	160	

$A_{FB}$  for (00)

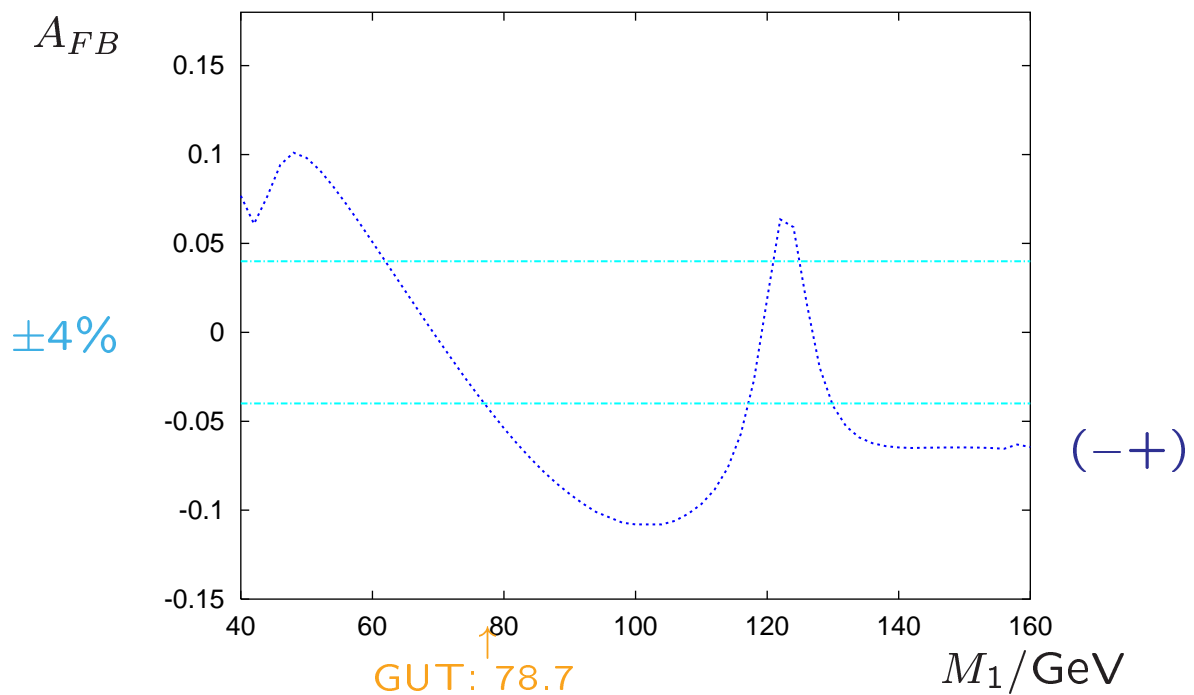
$$\sqrt{s} = m_{\tilde{\chi}_1^0} + m_{\tilde{\chi}_2^0} + 50 \text{ GeV}$$



- complex interplay between production and decay ( $\rightarrow$  spin correlations)
- $A_{FB}$  depends strongly on  $M_1$
- for  $\mathcal{L}^h$ : in  $M_1 < 58$  GeV and  $M_1 = [105, 135]$  GeV  
 $\Rightarrow A_{FB} \geq 4\%$

and  $(-+)$ :

$$\sqrt{s} = m_{\tilde{\chi}_1^0} + m_{\tilde{\chi}_2^0} + 50 \text{ GeV}$$



- **strong** dependence on beam polarization
- for  $\mathcal{L}^h$ : information from  $A_{FB} \geq 4\%$   
where  $A_{pol} \leq 4\%$ !

## 2.3 Influence of Slepton Masses: $m_{\tilde{e}_L} < m_{\tilde{e}_R}$

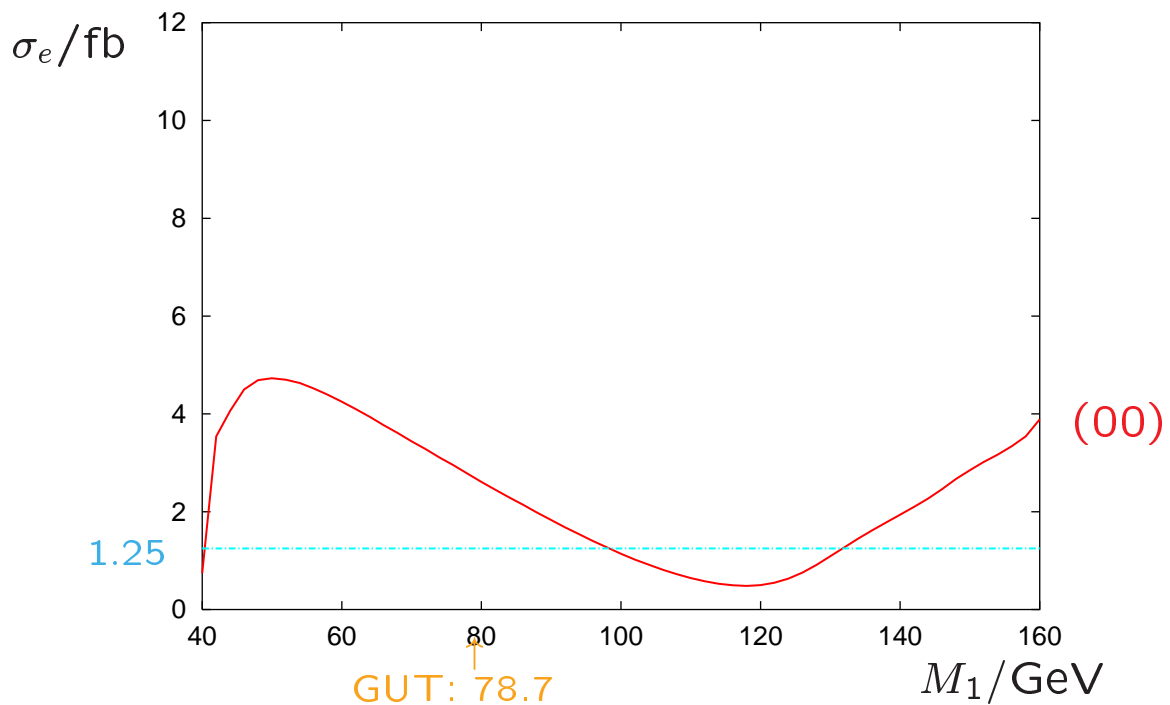
$M_1$  Dependence of  $\sigma_e$

$M_2$	$\mu$	$\tan \beta$	$m_{\tilde{e}_L}$	$m_{\tilde{e}_R}$
152	316	3	160	197

[mass]=GeV

Cross sections for (00):

$$\sqrt{s} = m_{\tilde{\chi}_1^0} + m_{\tilde{\chi}_2^0} + 50 \text{ GeV}$$



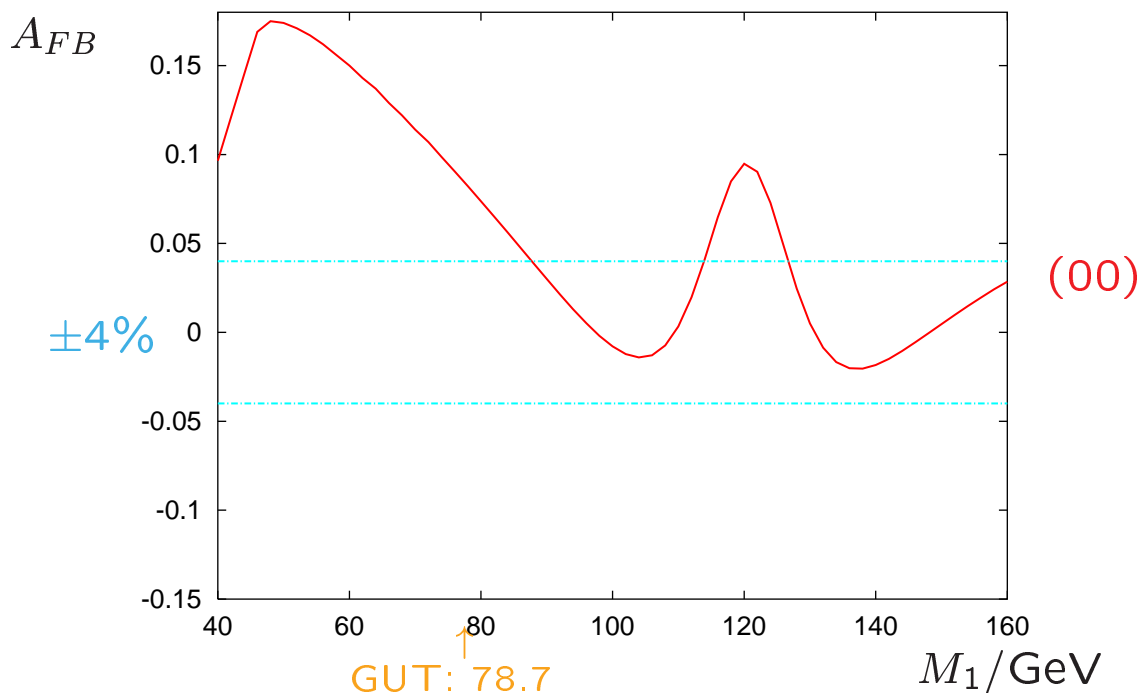
- $\sigma_e$  strongly influenced by **slepton masses**
- $M_1$  Dependence changes completely  
 $\Rightarrow$  Strong differences for  $\begin{pmatrix} m_{\tilde{e}_L}=197 \text{ GeV} \\ m_{\tilde{e}_R}=160 \text{ GeV} \end{pmatrix} \leftrightarrow \begin{pmatrix} m_{\tilde{e}_L}=160 \text{ GeV} \\ m_{\tilde{e}_R}=197 \text{ GeV} \end{pmatrix}$

## $M_1$ Dependence of $A_{FB}$ in lab-system

$M_2$	$\mu$	$\tan \beta$	$m_{\tilde{e}_L}$	$m_{\tilde{e}_R}$	[mass]=GeV
152	316	3	160	197	

$A_{FB}$  with (00):

$$\sqrt{s} = m_{\tilde{\chi}_1^0} + m_{\tilde{\chi}_2^0} + 50 \text{ GeV}$$



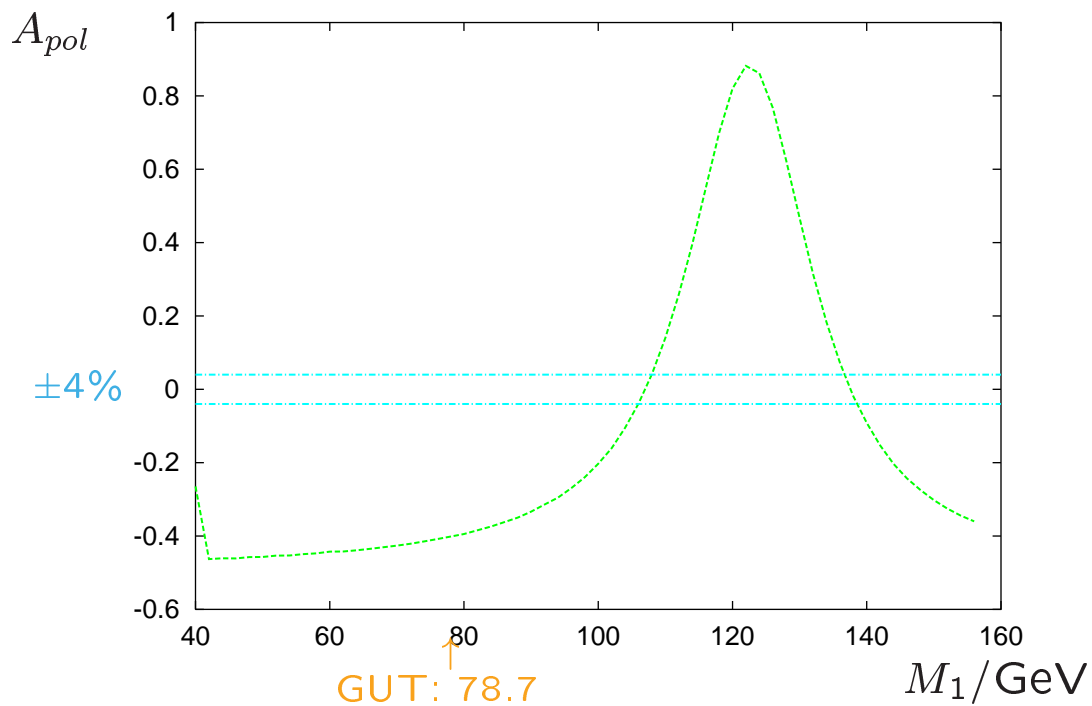
- $A_{FB}$  strongly influenced by **slepton masses**  
 $\Rightarrow$  larger  $A_{FB}$  possible
- $M_1$  Dependence of  $A_{FB}$  changes  
 $\Rightarrow$  Strong differences for  $\begin{pmatrix} m_{\tilde{e}_L}=197 \text{ GeV} \\ m_{\tilde{e}_R}=160 \text{ GeV} \end{pmatrix} \leftrightarrow \begin{pmatrix} m_{\tilde{e}_L}=160 \text{ GeV} \\ m_{\tilde{e}_R}=197 \text{ GeV} \end{pmatrix}$

# $M_1$ Dependence of Polarization Asymmetry

$M_2$	$\mu$	$\tan \beta$	$m_{\tilde{e}_L}$	$m_{\tilde{e}_R}$	[mass]=GeV
152	316	3	160	197	

$$A_{pol} := [\sigma_e(00) - \sigma_e(-+)] / [\sigma_e(00) + \sigma_e(-+)]$$

$$\sqrt{s} = m_{\tilde{\chi}_1^0} + m_{\tilde{\chi}_2^0} + 50 \text{ GeV}$$



- $A_{pol}$  **less** influenced by slepton masses  
(but dependent on slepton mass splitting!)

### 3. Conclusions

- Comparison of Extended Models
  - polarization effects completely **different** from MSSM ( $\Rightarrow$  *different couplings!*)
  - strong influence of **spin correlations** for gauginos
  - $A_{FB}$  of decay leptons **different** from MSSM
  - polarization of **both** beams useful
  - if light  $\tilde{S}$ : **high** luminosity essential
- $M_1$  Dependence in MSSM
  - $\sigma_e$ ,  $A_{pol}$  and  $A_{FB}$ :
    - show strong  $M_1$  Dependence due to influence on **couplings** and **masses**
    - Test of  $M_1/M_2$  GUT Relation
  - strongly influenced by:
    - **beam polarization**
    - **slepton masses**